

**ME103**:: Experimentation and Measurements

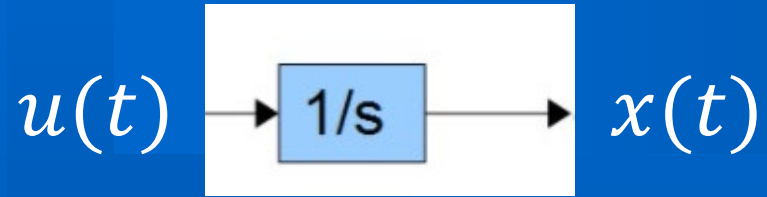
**Lecture #12**

## ME103:: Experimentation and Measurements

## Experimental Set-up Consultation

- 15-20 Minute consultation with staff on your instrument
- Please be ready with questions about how to prepare your test samples
- Understand what needs to be calibrated on your instrument
- Understand the range of operation of your experimental platform
- Make sure your experiments are designed to work within the parameters of the setup.

Bode Plot:



$$x(t) = \int_{0^-}^t u(t) dt$$

$$\frac{dx(t)}{dt} = u(t)$$

$$u(t) = \cos(\omega t)$$

$$x(t) = \frac{1}{\omega} \sin(\omega t) = \frac{1}{\omega} \cos\left(\omega t - \frac{\pi}{2}\right)$$

## Bode Plot:

Command Window

```
>> sys1 = tf([1],[1 0])
```

```
sys1 =
```

$$\frac{1}{s}$$

```
Continuous-time transfer function.
```

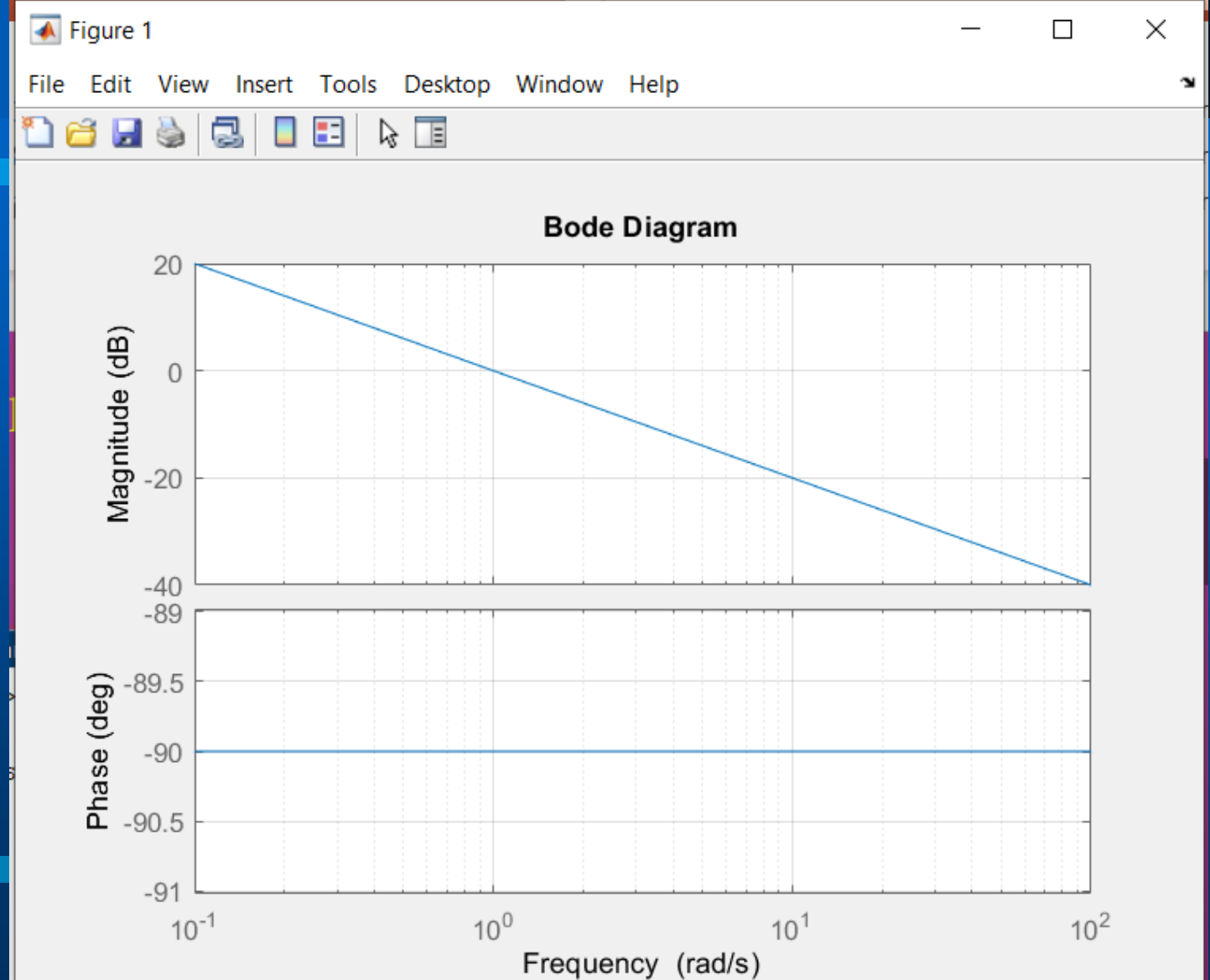
```
>> bode(sys1)
```

```
fx >> |
```

$$j\omega \rightarrow s$$

$$\frac{O(j\omega)}{I(j\omega)} = \left| \frac{1}{j\omega} \right|$$

$$M(j\omega) = 0 - \frac{1}{\omega}j$$



$$V_S(t) = V_A \cos(\omega(t) + \varphi)$$

Phasor Notations:

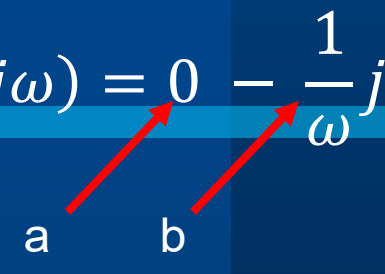
$$(1) \bar{V}_S = V_A \angle \varphi \quad \text{standard form} \quad (3) \bar{V}_S = V_A e^{j\varphi} \quad \text{exponential form}$$

$$(2) \bar{V}_S = a + jb \quad \text{complex form}$$

$$a = V_A \cos \varphi$$

$$b = V_A \sin \varphi$$

Converting complex to standard:

$$M(j\omega) = 0 - \frac{1}{\omega}j$$


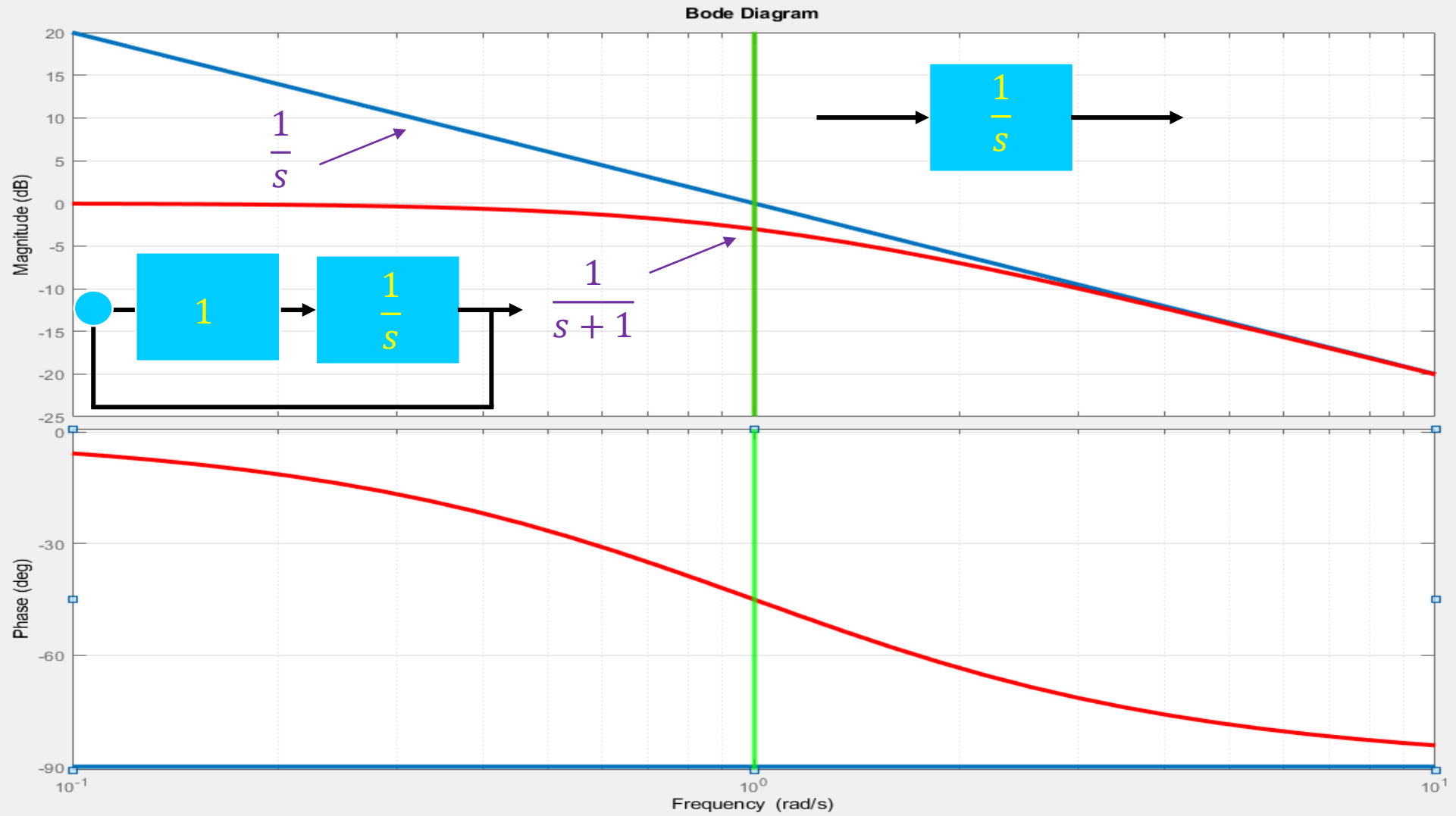
a

b

$$V_A = \sqrt{a^2 + b^2} = \sqrt{0^2 + \left(-\frac{1}{\omega}j\right)^2} = \left|\frac{1}{\omega}\right|$$

$$\varphi = \tan^{-1}\left(\frac{b}{a}\right) = \tan^{-1}\frac{-\frac{1}{\omega}}{0} = -\frac{\pi}{2}$$

# Using Bode Plot to design (Frequency Shaping):

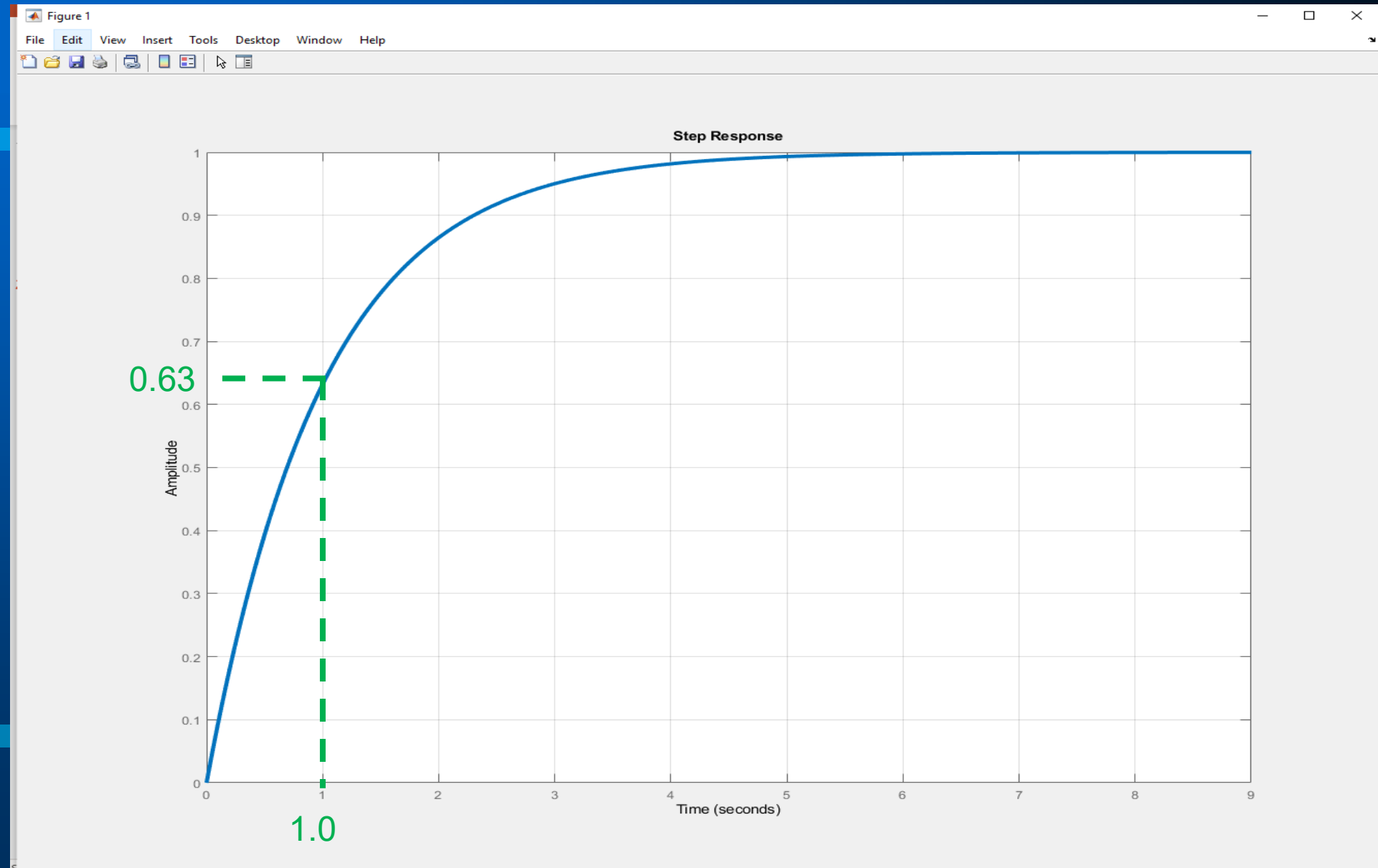


# Using Bode Plot to design (Frequency Shaping):

Closed Loop TF:

$$\frac{1}{s + 1}$$

$$c(t) = 1 - e^{-t}$$



## Using Bode Plot to design (Frequency Shaping):

@ $\omega = 1 \text{ rad/s}$

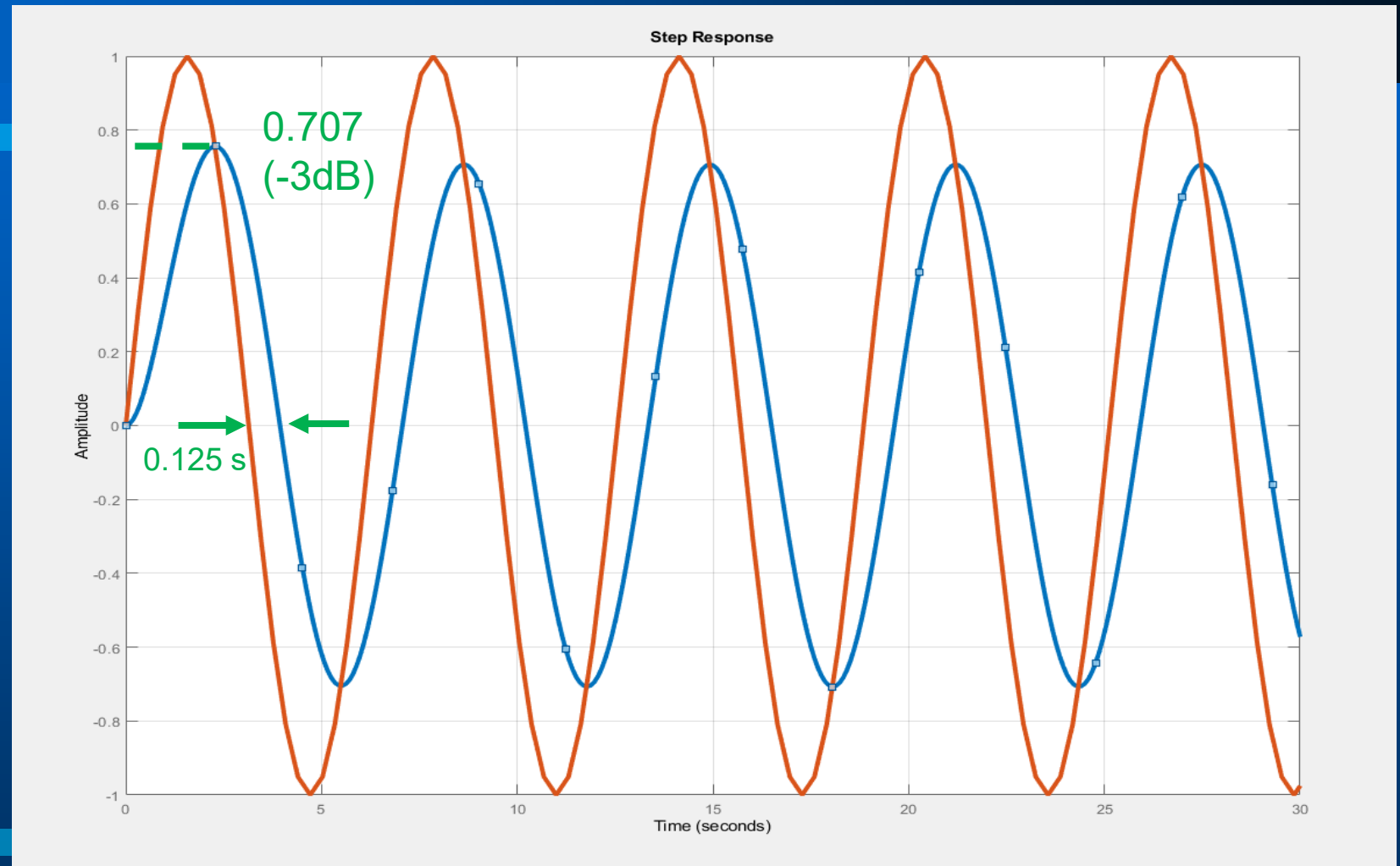
Open loop gain = 1

Closed loop gain = -3dB

Closed loop phase =  $-45^\circ$

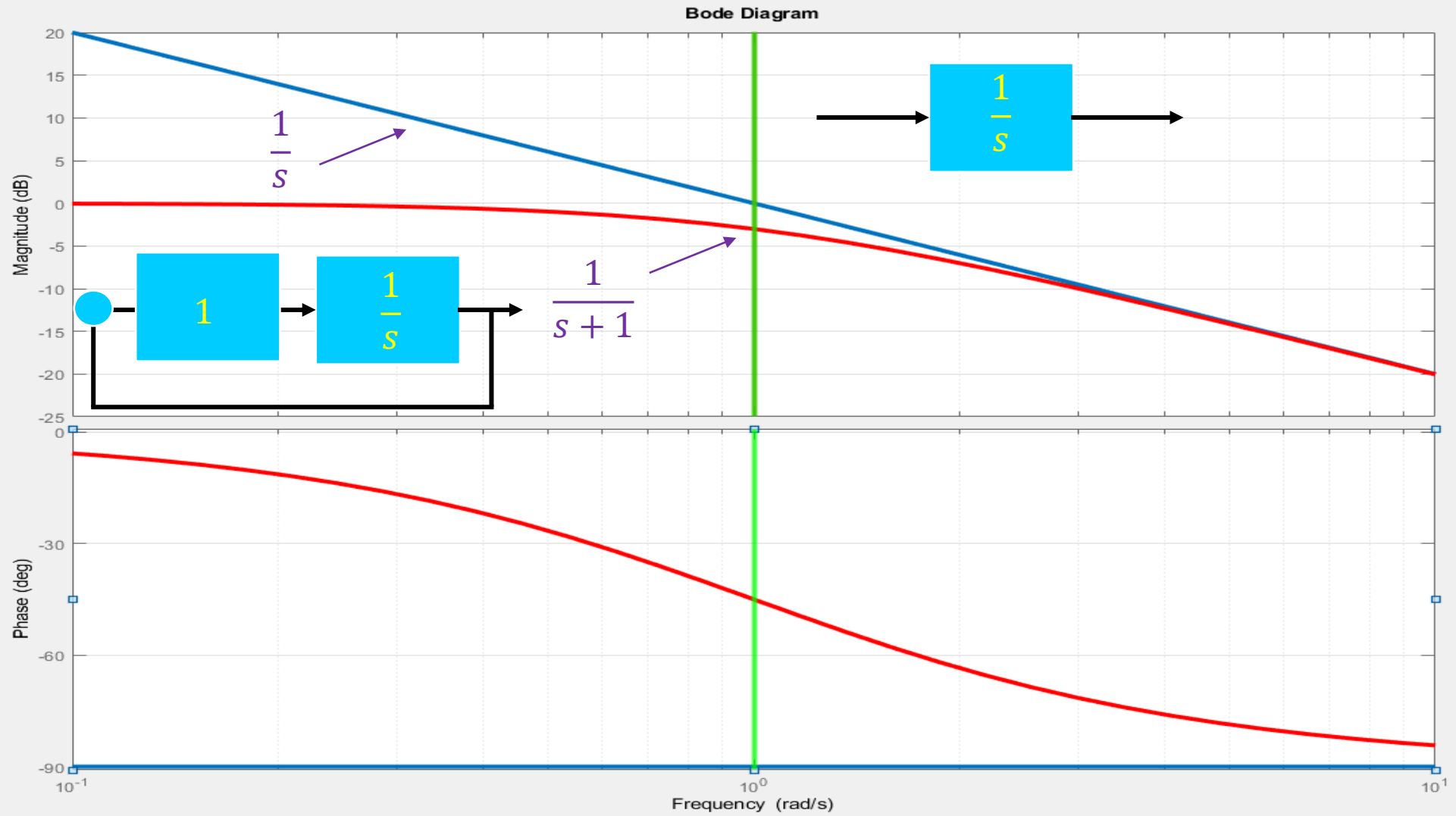
$$\Delta t = \frac{\Delta \phi}{360 * f}$$

$$\Delta t = \frac{45}{360 * 1} = 0.125 \text{ s}$$



- Positive phase difference → signal leads (occurs earlier)
- Negative phase difference → signal lags (occurs later)

# Using Bode Plot to design (Frequency Shaping):



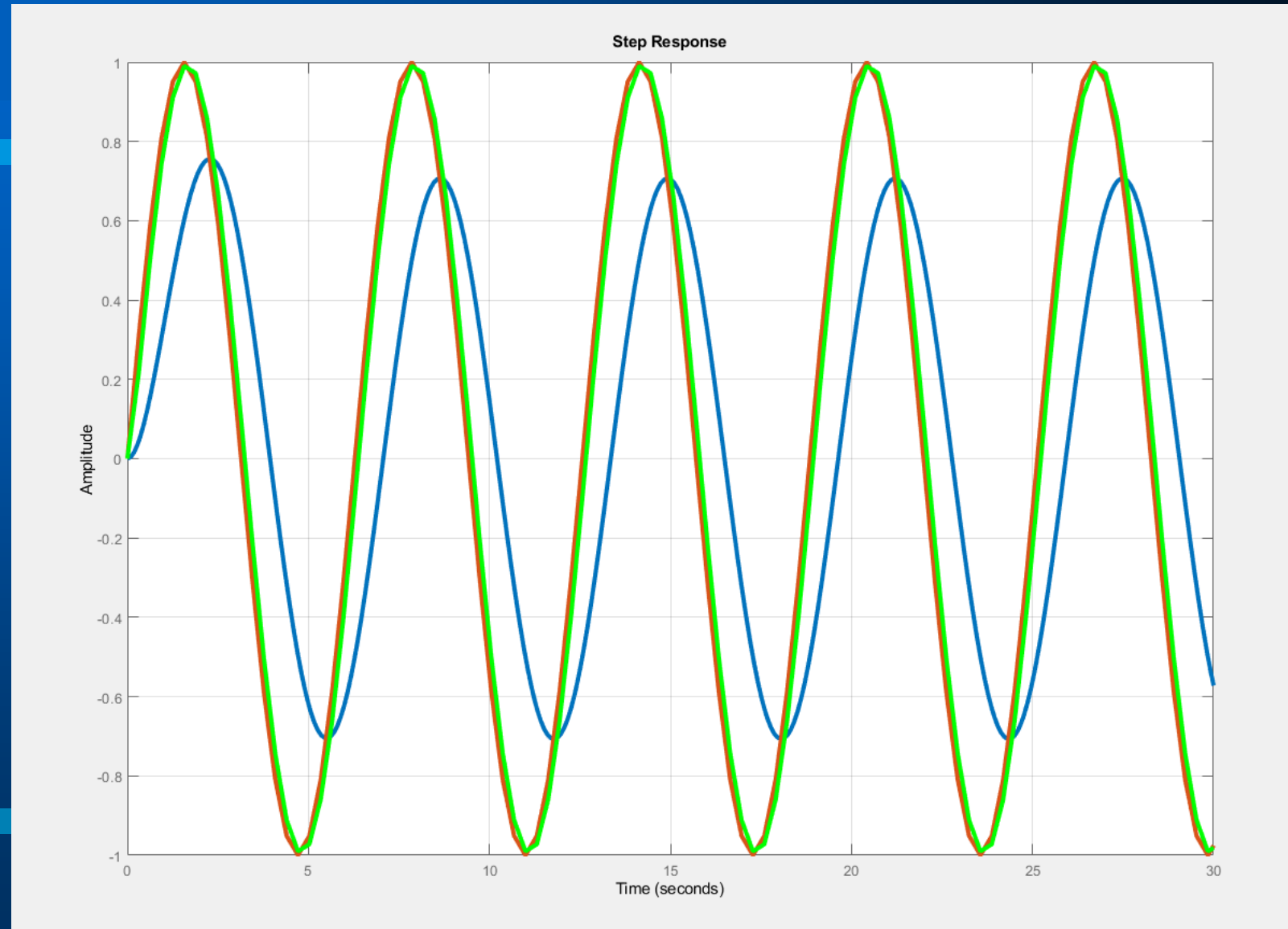
## Using Bode Plot to design (Frequency Shaping):

@ $\omega = 1 \text{ rad/s}$

Open loop gain = 10 = 1dB

Closed loop gain = -3dB

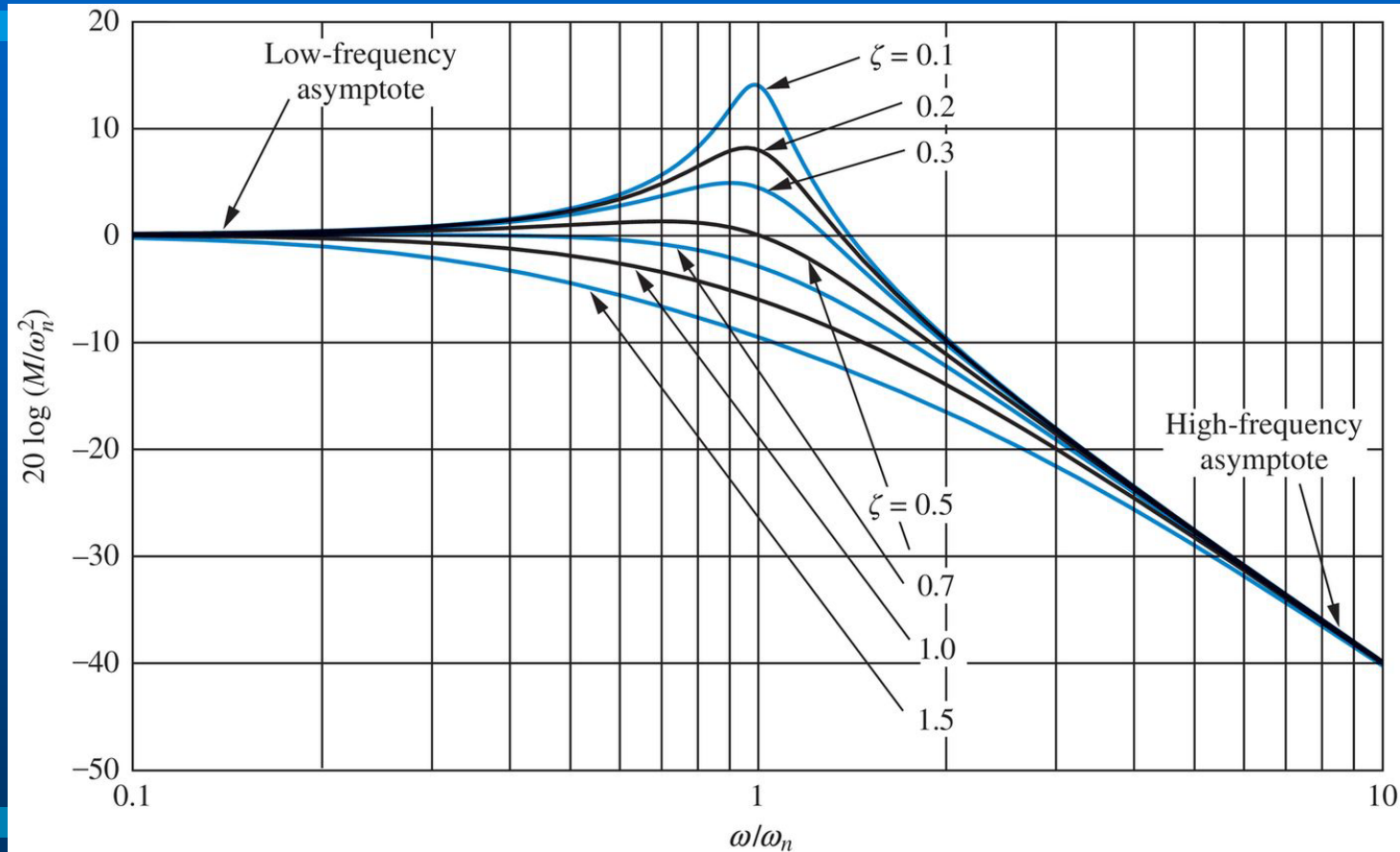
Closed loop phase =  $45^\circ$



## Bode Plot:

## Magnitude (Standard Form)

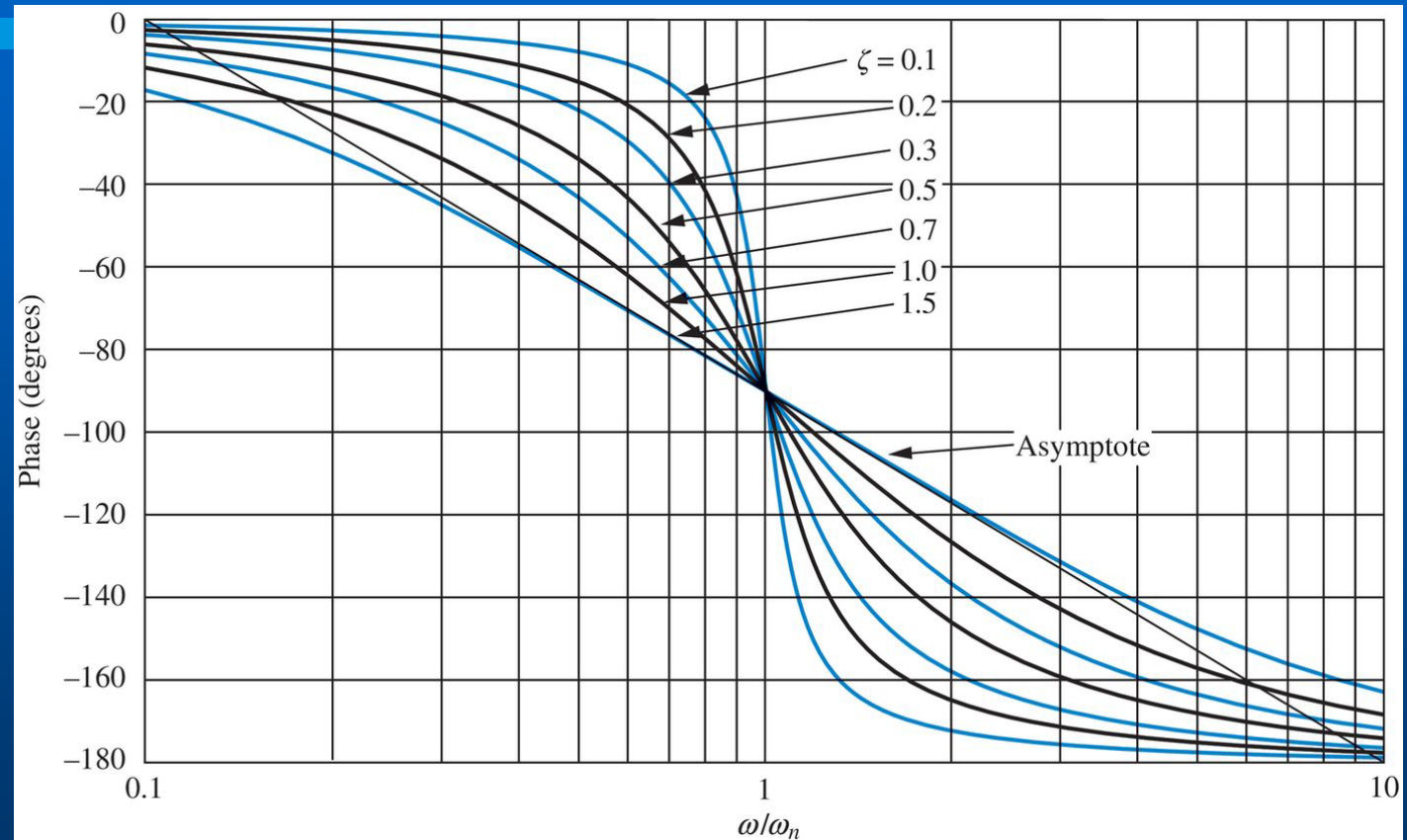
$$|G(j\omega)| = \frac{1/m}{\sqrt{(\omega_n^2 - \omega^2)^2 + (2\zeta\omega_n\omega)^2}}$$



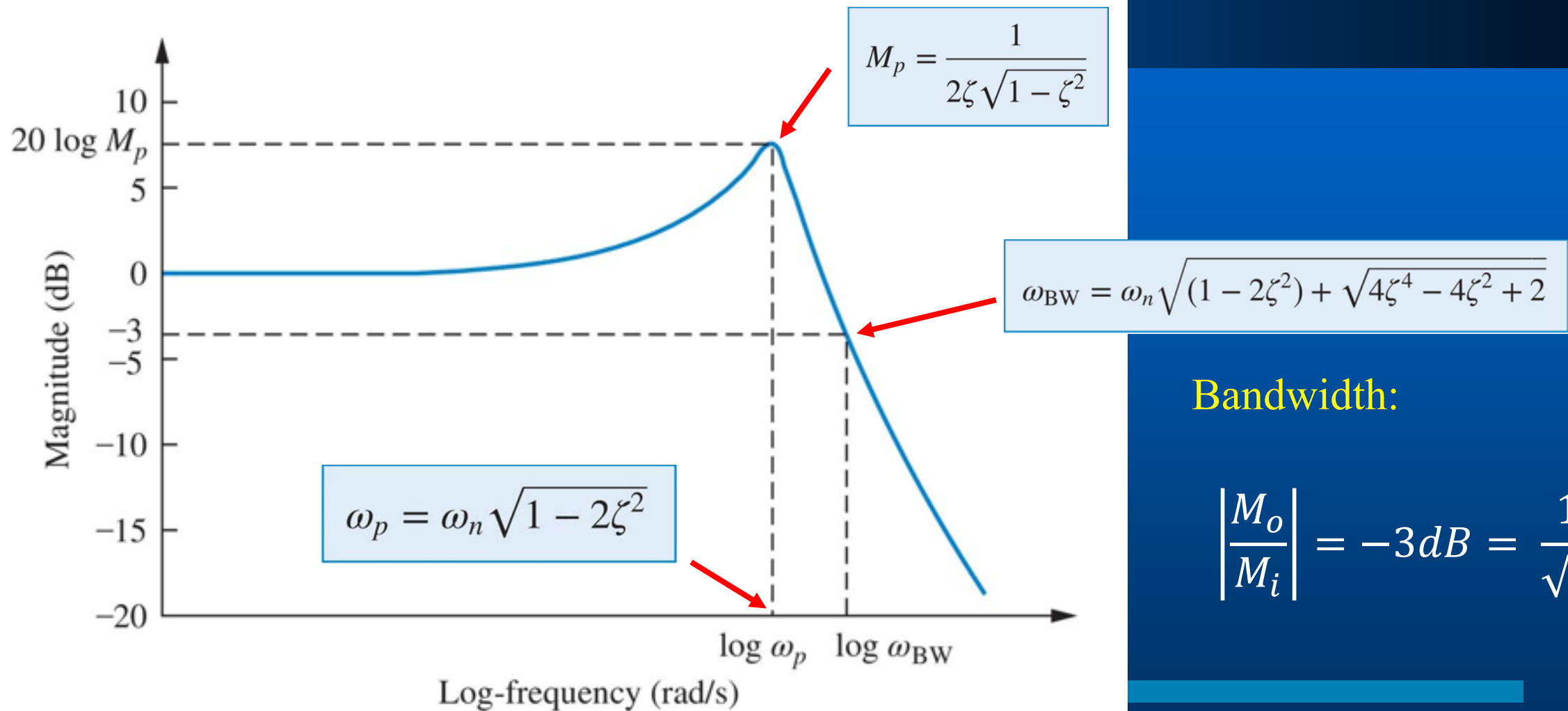
Bode Plot:

Phase (Standard Form)

$$\angle G(j\omega) = -\tan^{-1} \left( \frac{2\zeta\omega_n\omega}{\omega_n^2 - \omega^2} \right)$$



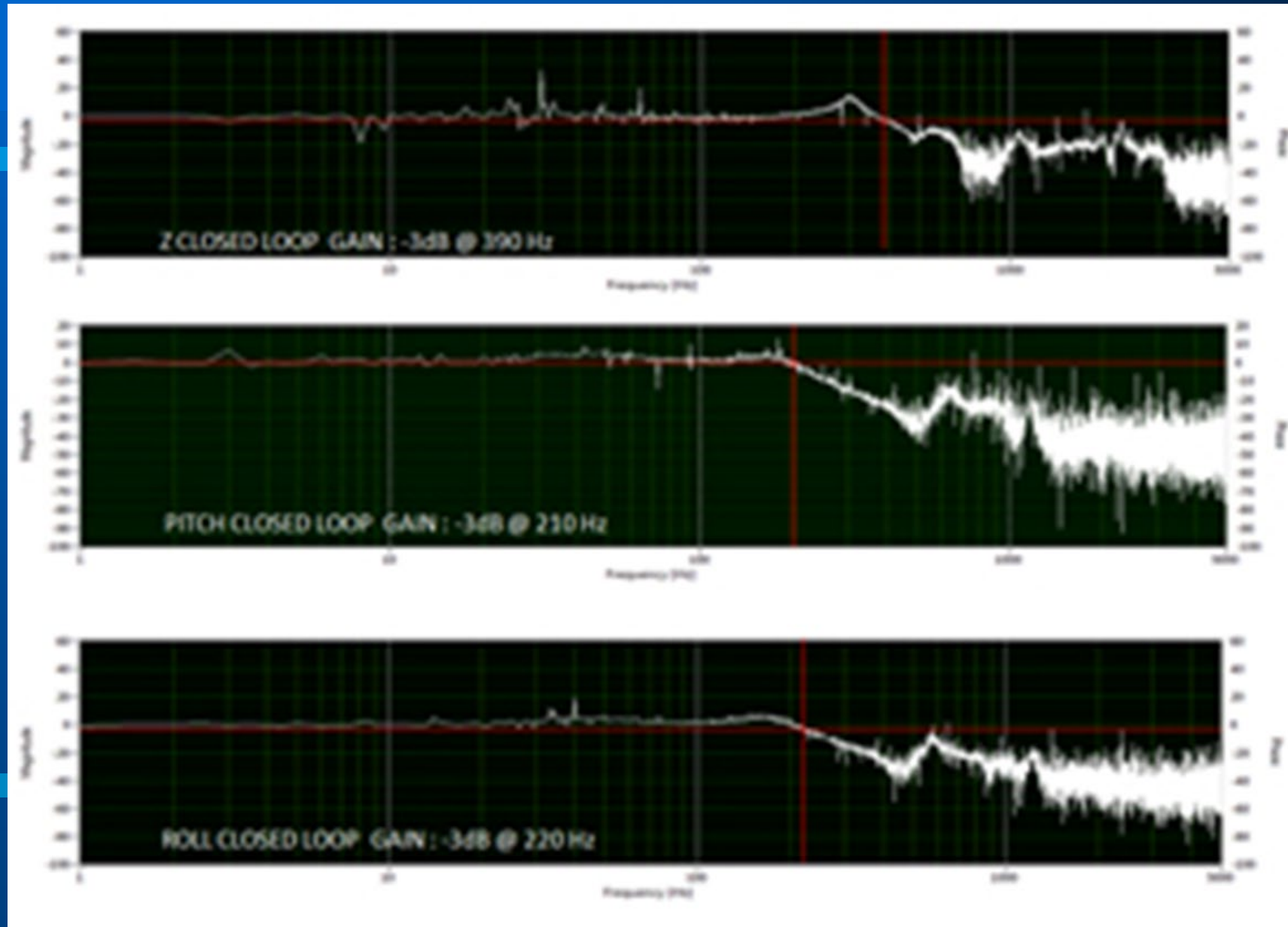
## Bode Plot:



## Bandwidth:

$$\left| \frac{M_o}{M_i} \right| = -3dB = \frac{1}{\sqrt{2}}$$

## Bode Plot:



# Bode Plot:

